ing very similar. The deposition could be explained by assuming adsorption of insoluble hydroxo forms of zinc onto the platinum foil.

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Department of Chemistry
University of Tennessee
Knoxville 16, Tennessee

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## The Hydrogen Bond. II. The Intramolecular Bond in Cyclic 1,2-Diols

By Lester P. Kuhn

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#### Abstract

The value of $\Delta \nu$, which is a measure of the length of the hydrogen bond, has been determined for a number of $c i s$ and trans cyclic 1,2-diols. The relationship between ring size and $\Delta v$ for both the cis and trans series is shown. In rings smaller than cyclodecane $O H$ groups are closer together in the cis than in the trans diols. In rings larger than cyclodecane the OH groups of the trans isomer are closer together than those of the cis. Some conclusions are drawn concerning the constellation of cyclic compounds, and evidence is adduced which supports H. C. Brown's I-strain theory of the chemical reactivity of cyclic compounds.


In part I of this series, ${ }^{1}$ it was shown that many dihydroxy compounds in dilute solution in carbon tetrachloride have two OH bands in the three-micron region. The higher frequency band is due to the free OH group and the lower frequency band is due to the bonded OH , indicating that these compounds exist in the form


The separation between the two bands, $\Delta \nu$, was found to increase as the length of the hydrogen bond decreases, thus in a series of closely related compounds where polarity differences are small, the observed values of $\Delta \nu$ can be used as a measure of the distance between the OH groups. In the work to be described here, this technique has been applied to a study of cyclic diols in which the $\mathrm{H}-\mathrm{O}$ distance is determined by the constellation of the ring. ${ }^{2}$

The orientation of the exocyclic bonds around an endocyclic $\mathrm{C}-\mathrm{C}$ bond is conveniently described by the angle $\phi$ which is defined as the angle formed by two exocyclic bonds as the observer looks down the axis of the $\mathrm{C}-\mathrm{C}$ bond. This is illustrated for the cyclic 1,2-diols in Fig. 1 where the solid lines represent the bonds of carbon atom number 1 and the dashed lines represent the bonds of carbon number 2 . The $\mathrm{C}-\mathrm{C}$ bond is perpendicular to the plane of the paper. The angle that is formed by an axial and an equatorial bond ${ }^{3}$ will be called $\phi_{\mathrm{a}}$, and the angle formed by two equatorial bonds will be called $\phi_{\mathrm{ee}}$.
The positions of the OH bands of the cis and trans isomers of cyclic 1,2 -diols containing $5,6,7,8,9$, 10, 12 and 16 carbon atoms were carefully determined. The values of $\Delta \nu$ are shown in Table I.
In using these data to draw conclusions concerning the constellation of the molecules studied, it is
(1) L. P. Kuhn, This Journal, 74, 2492 (1952).
(2) The term constellation is used to denote the geometric forms of cyclic compounds which arise by rotation around the $\mathrm{C}-\mathrm{C}$ bonds, thus the chair and the boat forms of cyclohexane are possible constellations of this molecule: V. Prelog, J. Chem. Soc., 423 (1950)
(3) It has been recommended that the two types of exocyclic bonds of cyclohexane, which have been previously called $\epsilon$ and K by some, and polar and equatorial by others, now be called axial and equatorial. This new nomenclature will be used here; D. H. R. Barton, O. Hassel, K. S. Pitzer and V. Prelog, Science, 119, 49 (1954).


trans.

Fig. 1.
necessary to assume that (a) differences in $\Delta \nu$ between members of the series are due to differences in $\mathrm{H}-\mathrm{O}$ distance, and (b) the bond angles and distances in the portion of each molecule containing the grouping - $\mathrm{CHOH}-\mathrm{CHOH}-$ are the same. This means that the differences in $\mathrm{H}-\mathrm{O}$ distance are due to differences in $\phi_{\mathrm{ae}}$ for the cis diols and in $\phi_{\mathrm{ee}}$ for the trans diols.

Table I
Band Separation of Cyclic 1,2-Diols

| Compound, -1,2-diol | $\Delta \nu$ in cm. ${ }^{-}$ | $\phi_{\text {a }}$, deg. | $\phi_{\text {ce }}$, deg. |
| :---: | :---: | :---: | :---: |
| cis-Cyclopentane | $61^{2}$ | 0 |  |
| trans-Cyclopentane | $0^{2}$ |  | $<120$ |
| cis-Cyclohexane | 38 | 50 |  |
| trans-Cyclohexane | 33 |  | 60 |
| cis-Cycloheptane | 44 | 42 |  |
| trans-Cycloheptane | 37 |  | 51 |
| cis-Cycloöctane | 51 | 33 |  |
| trans-Cycloöctane | 43 |  | 44 |
| cis-Cyclononane | 49 | 36 |  |
| trans-Cyclononane | 45 |  | 41 |
| cis-Cyclodecane | 44 | 42 |  |
| trans-Cyclodecane | 45 |  | 41 |
| cis-Cyclododecane | 38 | 50 |  |
| trans-Cyclododecane | 51 |  | 33 |
| cis-Cyclohexadecane | ${ }^{\text {b }}$ |  |  |
| rans-Cyclohexadecane | 50 |  | 34 |

${ }^{a}$ Values taken from previous paper. ${ }^{1}{ }^{b}$ Each band here was a doublet making it impossible to obtain an unambiguous value for $\Delta \nu$.

Using the methods of trigonometry, the relationship between $\phi$ and the $\mathrm{H}-\mathrm{O}$ distance was calculated and is shown graphically in Fig. 2. It was as-


Fig. 2.- $\mathrm{H}-\mathrm{O}$ distance versus $\phi$. The following values were used in calculating the $\mathrm{H}-\mathrm{O}$ distance: $\mathrm{C}-\mathrm{C}, 1.54$; $\mathrm{C}-\mathrm{O}, 1.42 ; \mathrm{O}-\mathrm{H}, 0.96 ; \quad \mathrm{O}-\mathrm{C}-\mathrm{C}$ angle, $109^{\circ} 28^{\prime} ; \mathrm{C}-\mathrm{O}-\mathrm{H}$ angle, $108^{\circ}$.
sumed in these calculations that the orientation of the OH group around the $\mathrm{C}-\mathrm{O}$ bond is such that the $\mathrm{H}-\mathrm{O}$ distance is a minimum. The observed values of $\Delta \nu$ were converted to $\mathrm{H}-\mathrm{O}$ distances by the relationship given in the previous paper, ${ }^{1}$ and the $\mathrm{H}-\mathrm{O}$ distances were expressed in terms of the angle $\phi$. These values are shown in Table I. Because of the assumptions on which the relationship between $\Delta \nu$ and $\mathrm{H}-\mathrm{O}$ distance are based, ${ }^{1}$ no claim is made for the absolute accuracy of the values of $\phi$, nevertheless it is felt that they represent in a


Fig. 3.-Curve A, trans diols; curve B, cis diols; curve C, $\left(60^{\circ}-\varphi_{n e}\right)+\left(60^{\circ}-\varphi_{\mathrm{er}}\right)$.
semiquantitative manner the variation of $\phi$ with ring size.

The relationship between $\Delta \nu$ and ring size is shown graphically in Fig. 3. In the trans series of compounds, $\Delta \nu$ increases with increasing ring size and reaches a limiting value at cyclododecane. This limiting value is slightly greater than the $\Delta \nu$ of D -butane-2,3-diol which is the open chain analog of the cyclic trans diols. In the cis series of compounds the curve is quite irregular. It goes through a minimum at $\mathrm{C}_{6}$, through a maximum at $\mathrm{C}_{8}$, and appears to reach a limiting value at $\mathrm{C}_{12}$ which is the same as $\Delta \nu$ of the open chain analog, meso-butane-2,3-diol. In rings containing less than 10 carbon atoms the cis substituents are closer together than the trans. In rings containing more than 10 carbon atoms, the trans substituents are closer than the cis.

For the $\mathrm{H}-\mathrm{O}$ distance to be decreased in the $c i s$ series of compounds from what it is in cyclohexane the rotation around the $\mathrm{C}-\mathrm{C}$ bond is such as to make the ring more planar as shown in Fig. 1, leading ultimately to the constellation in which $\phi_{\mathrm{ae}}=0$ and four contiguous carbon atoms are coplanar as in cyclopentane. The extent to which such a constellation can be achieved appears to be greater for the 8 - and 9 -membered rings than for the other sized rings. It is possible to picture constellations for cycloöctane and for cyclononane in which $\phi_{\mathrm{ae}}=$ 0 and in which the normal angles for the $\mathrm{C}-\mathrm{C}$ bonds prevail as shown below. The fact that the observed

values of $\Delta \nu$ for these diols correspond to angles of 33 and $36^{\circ}$ indicate that these constellations are not the correct representation of these molecules. These constellations require a close approach of carbon atoms 1 and 5 in cycloöctane and of 1 and 6 in cyclononane, when numbered as shown above. The OH bands of the cis and trans isomers of cyclo-octane-1,5-diol and of cyclonononane-1,6-diol have been examined. In each case only one OH band was observed, indicating that there is no intramolecular hydrogen bond in these diols.

To reduce the $\mathrm{H}-\mathrm{O}$ distance of the trans diols by rotation around the $\mathrm{C}-\mathrm{C}$ bond, the ring must be made more puckered as shown by the arrows in Fig. 1. As might be expected, the tendency to achieve a more puckered constellation increases with increasing size of the ring until the limiting value is reached at $\mathrm{C}_{12}$. At first glance it might appear anomalous that the $\mathrm{H}-\mathrm{O}$ distance in the larger rings is smaller for the trans diols than for the cis compounds. This is only because one is more
familiar with the chemistry of small ring compounds in which cis substituents are closer than trans. The smaller H-O distance in the trans diols of the larger rings can be explained in the following manner. The hydrogen bond, being an attractive force between the two OH groups, tends to decrease $\phi_{\mathrm{ae}}$ in the case of the cis diols and to decrease $\phi_{\mathrm{ee}}$ in the case of the trans diols. A decrease in $\phi_{\mathrm{ae}}$ brings the methylene groups closer together, whereas a decrease in $\phi_{\mathrm{ee}}$ brings the methylene groups closer to hydrogen atoms. Because the methylene group is larger than a hydrogen atom the repulsion between two methylene groups is larger than the repulsion between a methylene and a hydrogen, hence for a given expenditure of energy $\phi_{\text {ee }}$ can be made smaller than $\phi_{\mathrm{ae}}$. In rings smaller than cyclodecane the requirement that the normal carbon bond angle be maintained opposes the repulsion of the methylene groups and is the decisive factor in determining the relative values of $\phi_{\mathrm{ee}}$ and $\phi_{\mathrm{ae}}$.

The stability of a particular constellation is determined largely by two factors. The first is the requirement that the normal bond angles be maintained, and the second is that there be a minimum overlap of the van der Waals radii of the nonbonded atoms. The strain produced by these two factors has been called I-strain. ${ }^{4}$ In general, the latter requirement is best met when all the $\phi$ 's are $60^{\circ}$. In cyclohexane both requirements are met perfectly, but in many other rings the former requirement causes one or more of the $\phi$ 's to deviate from $60^{\circ}$. In the case of the cyclic 1,2 -diols a decrease in $\phi$ will be accompanied by an increase in stability due to the strengthening of the hydrogen bond, hence the OH groups of the cis diols will be attached to the C-C group which has the smallest $\phi_{\mathrm{ae}}$, and the OH groups of the trans diols will be attached to the $\mathrm{C}-\mathrm{C}$ which has the smallest $\phi_{\mathrm{ee}}$. Thus we know the orientation around the two $\mathrm{C}-\mathrm{C}$ bonds of each ring. For example, from the data in Table I we can conclude that the constellation of the cycloöctane ring is such that the smallest $\phi_{\mathrm{ae}}$ is no less than approximately $33^{\circ}$ and the smallest $\phi_{\mathrm{ee}}$ is no less than approximately $44^{\circ}$. A complete description of the constellation of a ring would require the knowledge of $\phi_{\mathrm{ae}}$ or $\phi_{\mathrm{ee}}$ associated with each $\mathrm{C}-\mathrm{C}$ bond.

An attempt will now be made to correlate the data in Fig. 3 with chemical reactivity. The relationship between chemical reactivity and ring size for two different types of reactions is shown in Fig. 4. Curve A, taken from the work of V. Prelog, ${ }^{2}$ shows the effect of ring size on the equilibrium constant for the dissociation of cyclic cyanhydrins,

$$
\left(\underset{\sim}{C} \mathrm{C}_{2}\right)_{n} \mathrm{C}(\mathrm{OH}) \mathrm{CN}=\underset{\left.\mathrm{C}_{2}\right)_{n} \mathrm{C}}{\Gamma}=\mathrm{O}+\mathrm{HCN}
$$

Curve B, taken from the work of Brown and Borkowski, ${ }^{4}$ shows the effect of ring size on the rate constant for the unimolecular solvolysis of methyl cycloalkyl chlorides. The similarity between the curves in Fig. 4 and the curve for the cis compounds in Fig. 3 is so striking that it strongly suggests a common basis of explanation, namely, the variation of $\phi$. The observed effect of ring size on chemical
(4) H. C. Brown and M. Borkowski, This Journal, 74, 1894 (1952).


Fig. 4.-Curve A, equilibrium constant for the reaction $\left(\stackrel{\stackrel{\mathrm{CH}}{2})_{n}}{ } \mathrm{C}(\mathrm{OH}) \mathrm{CN} \rightleftarrows\left(\stackrel{\Gamma}{\left.\mathrm{CH}_{2}\right)_{n}} \mathrm{C}=0+\mathrm{HCN}\right.\right.$. Curve B, first-order rate constant for the solvolysis of $\left(\mathrm{CH}_{2}\right)_{n} \mathrm{CMeCl}$.
reactivity has been explained by $\mathrm{H} . \mathrm{C}$. Brown ${ }^{4}$ on the basis of I-strain. Those reactions will go more readily which are accompanied by a decrease in Istrain. The conversion of cyclohexanone to its cyanhydrin is accompanied by a decrease in Istrain, whereas the same reaction with cyclopentanone is accompanied by an increase in I-strain, hence the former equilibrium constant for the dissociation of the cyanhydrin should be the smaller as shown in Fig. 4. Similarly, in the SN1 reaction in which the rate-determining step is the formation of a carbonium ion, there will be a much larger increase in I-strain of the cyclohexyl compound than of the cyclopentyl compound, hence the former should react more slowly.

Let us now consider how I-strain, insofar as it is produced by the overlap of van der Waals radii of non-bonded atoms on adjacent carbon atoms, is related to the values of $\phi_{\mathrm{ae}}$ and $\phi_{\mathrm{ee}}$ given in Table I. As stated earlier, I-strain is a minimum when $\phi=$ $60^{\circ}$, so that the deviation of the observed $\phi_{\mathrm{ae}}$ and $\phi_{e \mathrm{e}}$ from $60^{\circ}$ will be a measure of I-strain. In Fig. 3 , curve C , the term $\left(60-\phi_{\mathrm{ae}}\right)+\left(60-\phi_{\mathrm{ee}}\right)$ is plotted against ring size. The similarity between this curve and the curves in Fig. 4 supports Brown's I-strain theory and substantiates the belief that the overlap of the van der Waals radii of non-bonded atoms makes a major contribution to the I-strain. The I-strain will be the summation of the effects produced by the orientation around each of the $\mathrm{C}-\mathrm{C}$ bonds whereas the data in Table I relate to only two $\mathrm{C}-\mathrm{C}$ bonds of each ring. Since the smallest $\phi_{\mathrm{ae}}$ and $\phi_{\mathrm{ee}}$ will make the largest contribution to the I-strain, it is to be expected that the term used in Fig. 3 curve $C$ will be an approximate measure of I-strain.

The rate of oxidation of glycols by lead tetraacetate according to the equation

$$
\begin{aligned}
& \mathrm{RCHOH}-\mathrm{CHOHR}+\mathrm{Pb}(\mathrm{OAC})_{4}= \\
& 2 \mathrm{RCHO}+2 \mathrm{AcOH}+\mathrm{Pb}(\mathrm{OAC})_{2}
\end{aligned}
$$

was believed at one time to depend upon the distance between the OH groups. This belief was based upon the observations that the rate of oxidation of the cis 1,2-diols of cyclopentane and cyclo-
hexane is greater than that of the trans isomers. ${ }^{5}$ The rates of oxidation of certain cyclic glycols were taken from the literature ${ }^{6}$ and are shown in Table II. In four of the six pairs of isomers for which data are available, the isomer in which the OH groups are closer together also reacts more quickly with $\mathrm{Pb}(\mathrm{OAc})_{4}$. A comparison of the data with the data in Table I shows that there is no simple correlation between the reaction rates and $\Delta \nu$, which indicates that the distance between the OH groups is not the major factor that determines the reaction rate.

The ability of 1,2 -diols to react with acetone to form cyclic ketals according to the equation

$$
\begin{aligned}
\mathrm{RCHOH}-\mathrm{CHOHR}+\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CO} & = \\
& \mathrm{RCH}-\mathrm{O} \\
& \mathrm{RCH}-\mathrm{O}
\end{aligned}>{\mathrm{C}\left(\mathrm{CH}_{3}\right)_{2}+\mathrm{H}_{2} \mathrm{O}}^{2}
$$

appears to be related to the distance between the OH groups. Only qualitative data could be found in the literature. These data are given in the last column of Table II, where + indicates that reac-

Table II

| Reactivity of CyClic Diols |  |  |
| :--- | :---: | :---: |
| Compound, -1,2-diol | With $\mathrm{Pb}(\mathrm{OAc})_{4}{ }^{2}$ | With acetone |
| cis-Cyclopentane | 40,000 | + |
| trans-Cyclopentane | 12.8 | - |
| cis-Cyclohexane | 5 | + |
| trans-Cyclohexane | 0.2 | - |
| cis-Cycloheptane |  | + |
| trans-Cycloheptane |  | + |
| cis-Cycloöctane |  | + |
| trans-Cycloöctane | 2.87 | + |
| cis-Cyclononane | 20.7 | + |
| trans-Cyclononane | 2.6 | + |
| cis-Cyclodecane | 100 | + |
| trans-Cyclodecane | 1.27 |  |
| cis-Cyclododecane | 73.6 |  |
| trans-Cyclododecaile | 7.84 |  |
| cis-Cyclohexadecane | 91.2 |  |
| trans-Cyclohexadecane |  |  |

"The figures in this column are the second-order rate constants for reaction in glacial acetic acid, $k^{20}$ (mole ${ }^{-1} 1$. min..$^{-1}$ ).

[^0]tion takes place and - indicates that no reaction takes place. Comparison of these data with Table I shows that compounds with a $\Delta \nu$ greater than 36 react with acetone and compounds with a $\Delta \nu$ less than 34 do not react.
Experimental.-The purity of the diols was determined by their melting points. In each case the melting point checked with that in the literature. Solutions of 0.005 molarity or less for the less soluble compounds in reagent grade $\mathrm{CCl}_{4}$, which had been dried and distilled over $\mathrm{P}_{2} \mathrm{O}$ :, were used. The absorption curves were obtained with a PerkinElmer double-beam spectrometer, which was equipped with a LiF prism, and which was purged with dry nitrogen while in use. The slit width was 25 microns and the cell length was 2 cm . A $2-\mathrm{cm}$. cell containing pure $\mathrm{CCl}_{4}$ was used in the reference beam. The band widths at minimum transmission varied from less than 1 to $5 \mathrm{~cm} .^{-1}$. The center of the band at the transmission minimum was chosen as the position of the band. The value of the $\%$ transmission at the transmission minimum varied from 15 to $40 \%$. In each case there was no large difference between the intensities of the free OH and the bonded OH bands.
The frequencies of all the compounds studied are given in Table III.

Table III

| Compound, -1,2-diol | Free OH | Bonded OH |
| :---: | :---: | :---: |
| cis-Cyclohexane | 3626 | 3588 |
| trans-Cyclohexane | 3633 | 3600 |
| cis-Cycloheptane | 3632 | 3588 |
| trans-Cycloheptane | 3626 | 3589 |
| cis-Cycloöctane | 3635 | 3584 |
| trans-Cycloöctane | 3631 | 3588 |
| cis-Cyclononane | 3631 | 3582 |
| trans-Cyclononane | 3632 | 3587 |
| cis-Cyclodecane | 3629 | 3585 |
| trans-Cyclodecane | 3633 | 3588 |
| cis-Cyclododecane | 3629 | 3591 |
| trans-Cyclododecane | 3635 | 3584 |
| cis-Cyclohexadecane | 3632, 3626 | 3591,3587 |
| trans-Cyclohexadecane | 3635 | 3585 |
| cis-Cyclononane | 3627 |  |
| trans-Cyclononane | 3627 |  |
| cis-Cycloöctane-1,5-diol | 3627 |  |
| trans-Cycloöctane-1, $\overline{0}$-diol | 3627 |  |

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Aberdeen Proving Ground, Md.


[^0]:    (5) R. Criegee, E. Bucher and W. Walther, Ber., 73, 571 (1940).
    (f) (a) V. Prelog, K. Schenker and W. Kung, Helv. Chim. Acta, 36, 471 (1953); (b) V. Prelog, K. Schenker and H. Gunthard, ibid., 35, 1598 ( 1952 ); (c) the data on the cyclododecanediols and the cyclohexadecanediols were kindly supplied in advance of publication by Professor Prelog.

